

**Topics :** Inverse Trigonometric Function, Matrices & Determinants, Fundamentals of Mathematics, Trigonometric Ratio, Function, Quadratic Equation

**Type of Questions**

**Single choice Objective (no negative marking)** Q.1,2,3,4,5,6 (3 marks, 3 min.)

**M.M., Min.**

**Subjective Questions (no negative marking)** Q.7,8 (4 marks, 5 min.)

[18, 18]

[8, 10]

1. The set of values of  $a$  for which  $x^2 + ax + \sin^{-1}(x^2 - 4x + 5) + \cos^{-1}(x^2 - 4x + 5) = 0$  has at least one solution is

(A)  $(-\infty, -\sqrt{2\pi}] \cup [\sqrt{2\pi}, \infty)$       (B)  $(-\infty, -\sqrt{2\pi}) \cup (\sqrt{2\pi}, \infty)$   
 (C)  $\mathbb{R}$       (D) none of these

2. If  $A$  is a square matrix of order 3 such that  $|A| = 2$ , then  $|\text{adj } A^{-1}|$  is :

(A) 2      (B) 4      (C)  $\frac{1}{2}$       (D)  $\frac{1}{4}$

3. If  $A = \begin{bmatrix} \alpha^2 & \alpha \\ \beta^2 & \beta \end{bmatrix}$ ,  $B = \begin{bmatrix} 6 \\ -5 \end{bmatrix}$ ,  $C = \begin{bmatrix} -1 \\ -1 \end{bmatrix}$  are such that  $AB = C$ , then absolute value of  $|A|$  is

(A)  $\frac{1}{6}$       (B) -30      (C)  $\frac{2}{27}$       (D)  $\frac{1}{36}$

4. If  $\sin^2 x + \sin x = 1$ , then  $\cos^{12} x + 3 \cos^{10} x + 3 \cos^8 x + \cos^6 x - 1$  is equal to  
 (A) 1      (B) 0      (C) -1      (D) none of these

5. Domain of the function  $f(x) = \log\left(\sin^{-1}\sqrt{x^2 + 3x + 2}\right)$  is

(A)  $(-\infty, -2) \cup (-1, \infty)$       (B)  $\left(-\frac{3-\sqrt{5}}{2}, \frac{-3+\sqrt{5}}{2}\right)$

(C)  $\left[\frac{-3-\sqrt{5}}{2}, -2\right] \cup \left(-1, \frac{-3+\sqrt{5}}{2}\right)$       (D) none of these

6. If  $\tan \alpha, \tan \beta, \tan \gamma$  are the roots of the equation  $x^3 - px^2 - r = 0$ , then the value of  $(1 + \tan^2 \alpha)(1 + \tan^2 \beta)(1 + \tan^2 \gamma)$  is equal to  
 (A)  $(p - r)^2$       (B)  $1 + (p - r)^2$       (C)  $1 - (p - r)^2$       (D) none of these

7. Find the domain of the following

(i)  $f(x) = \sqrt{x + \sqrt{x-1}}$       (ii)  $f(x) = \frac{\sqrt{\sin x}}{1 + \sec^2 x}$   
 (iii)  $f(x) = \log_2 \log_{|x+1|} (\sqrt{x-3})$       (iv)  $f(x) = \sin^{-1}(x^2 - x - 1) + \tan^{-1}(x^2 - 5x + 6) + \log_{x-2} |x^2 - 9|$

8. (i) Find the largest integral value of  $x$  which satisfies the inequality  $\frac{4x+19}{x+5} < \frac{4x-17}{x-3}$ .

(ii) Solve for  $x$  :  $\sqrt{\frac{x-2}{1-2x}} > -1$

# Answers Key

1. (D)      2. (D)      3. (D)      4. (B)

5. (C)      6. (B)

7. (i)  $[1, \infty)$

(ii)  $x \in [2n\pi, 2n\pi + \pi] - (2n + 1) \frac{\pi}{2}, n \in \mathbb{I}$

(iii)  $(4, \infty)$       (iv)  $\emptyset$

8. (i)  $x = 2$       (ii)  $(1/2, 2]$

